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# The structure and stability of $\mathbf{B}_{36} \mathbf{N}_{\mathbf{3 6}}$ cages: a computational study 

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#### Abstract

The structure and stability of $22 \mathrm{~B}_{36} \mathrm{~N}_{36}$ cage molecules containing four-membered $\left(F_{4}\right)$, five-membered $\left(F_{5}\right)$, six-membered $\left(F_{6}\right)$, eight-membered ( $F_{8}$ ) and 12-membered ( $F_{12}$ ) rings have been computed at the B3LYP $/ 6-31 G^{*}$ level of density functional theory. The most stable structure (1) has $T_{\mathrm{d}}$ symmetry with six $F_{4}$ and $32 F_{6}$ rings, following the isolated square rule, while the fullerene-like structures ( $12 F_{5}$ and $26 F_{6}$ ) and also structures with $F_{8}$ and $F_{12}$ are much higher in energy.


Keywords DFT • Inorganic fullerene • Structure • Stability

## Introduction

Stoichiometric boron nitrides $(\mathrm{BN})_{\mathrm{n}}$, the isoelectronic analogues to carbon fullerenes, have been a subject of extensive and intensive investigations. In contrast to carbon fullerenes ( $\mathrm{C}_{60}$ and $\mathrm{C}_{70}$ ), there is no direct evidence for the most favored structures of BN analogues, despite advanced synthesis and characterization [1-11]. In contrast, recent advances and developments in theoretical methods and computer technology provide an alternative tool for elucidating the structure and stability of $(\mathrm{BN})_{\mathrm{n}}$.

[^0]While the stability of carbon fullerenes is governed by the isolated pentagon rule (IPR), i.e., the maximal and perfect separation of the strained pentagons, the stability of $(\mathrm{BN})_{\mathrm{n}}$ can be estimated by the isolated square rule (ISR), i.e., the maximal and perfect separation of the strained squares. In 1993, Jensen and Toftlund [12] carried out ab initio calculations on two $\mathrm{B}_{12} \mathrm{~N}_{12}$ clusters, and found that the isomer with squares and hexagons is more stable than that with pentagons and hexagons by $210 \mathrm{kcal} \mathrm{mol}^{-1}$, while just the opposite energetic order is found for the corresponding $\mathrm{C}_{24}$ isomers by $22 \mathrm{kcal} \mathrm{mol}^{-1}$ at the MP2/ DZP level of theory [12]. The enhanced stability of $\mathrm{B}_{12} \mathrm{~N}_{12}$ is ascribed to the absence of the less favored $\mathrm{B}-\mathrm{B}$ and $\mathrm{N}-\mathrm{N}$ bonds generally. Also in 1993, Haiduc and co-authors [13] studied the structures and stability of a set of alternating boron-nitrogen cages $(\mathrm{BN})_{\mathrm{n}}$ and pointed out the relationship between the number of the squares and hexagons. This relationship was further validated systematically by Sun et al. [14, 15] in 1995 on large cages (up to $\mathrm{B}_{41} \mathrm{~N}_{41}$ ).

Further systematic study on the structure and stability of $(\mathrm{BN})_{\mathrm{n}}(n=10-30)$ composed entirely of squares and hexagons was carried out by Seifert et al. [16] in 1997 at the density-functional tight-binding level of theory (DFTB), and they found that the alternant structures $\mathrm{B}_{12} \mathrm{~N}_{12}, \mathrm{~B}_{16} \mathrm{~N}_{16}$ and $\mathrm{B}_{28} \mathrm{~N}_{28}$ are "magic" with anomalous stability, which correlates with their large HOMOLUMO gaps.

However, the stability of the alternant $(\mathrm{BN})_{\mathrm{n}}$ structures over the fullerene structures has been questioned by Rogers et al. [17] on the basis of systematic DFTB calculations on a wider range of cluster sizes ( $n=10-35$ ). They found that the most stable fullerene structures with three $\mathrm{N}-\mathrm{N}$ and three $\mathrm{B}-\mathrm{B}$ bonds are more stable than the corresponding most stable alternant isomers over the entire range of the cluster sizes. The origin for this energetic relationship has been ascribed to the competing forces of chemical (three $\mathrm{B}-\mathrm{B}$ and $\mathrm{N}-\mathrm{N}$ bonds) and steric (six squares) frustrations. They pointed that this relationship also exists for large clusters like $(\mathrm{BN})_{36}$ and $(\mathrm{BN})_{72}$. For example, the alternant isomer of $(\mathrm{BN})_{36}$ in $T_{d}$ symmetry is higher in energy than the three most stable
fullerene-like (two oblates/ $C_{3}$, one prolate/ $D_{3}$ ) isomers by $140.8,98.5$ and $170.1 \mathrm{kcal} \mathrm{mol}^{-1}$, respectively, and the alternant $(\mathrm{BN})_{72}$ in $T$ symmetry is higher in energy than the most stable fullerene cage in $C_{3}$ symmetry by $161.0 \mathrm{kcal} \mathrm{mol}^{-1}$, and the least stable fullerene cage in $C_{3}$ symmetry by $83.0 \mathrm{kcal} \mathrm{mol}^{-1}$.

In contrast to the DFTB results by Rogers et al. [17] B3LYP density functional calculations on $(\mathrm{BN})_{\mathrm{n}}(n=$ $12-14,16,24$ ) [18-20] predicted that the alternant isomers are more stable than the fullerene isomers, e.g., $230 \mathrm{kcal} \mathrm{mol}^{-1}$ for (BN) 12 ( $210 \mathrm{kcal} \mathrm{mol}^{-1}$ at MP2/ DZP) [12] $136 \mathrm{kcal} \mathrm{mol}^{-1}$ for (BN) ${ }_{13}, 160 \mathrm{kcal} \mathrm{mol}^{-1}$ for $(\mathrm{BN})_{14}$ and $200 \mathrm{kcal} \mathrm{mol}^{-1}$ for $(\mathrm{BN})_{16}$ and $149 \mathrm{kcal} \mathrm{mol}^{-1}$ for $(\mathrm{BN})_{24}$, respectively. It is notable that the energy span for the most stable $(\mathrm{BN})_{\mathrm{n}}$ structure between DFTB and B3LYP is more than $300 \mathrm{kcal} \mathrm{mol}^{-1}$, and therefore too large simply to be ascribed to the effects of insufficiency in methods or basis sets.

In addition to this controversy in the stability of $(\mathrm{BN})_{\mathrm{n}}$ clusters, Pokropivny et al. [21] reported a $\mathrm{B}_{24} \mathrm{~N}_{24}$ structure with 12 squares, eight hexagons and six octagons in $O$ symmetry to be the lowest of any other near spherical molecules. They also reported that the most stable $\mathrm{B}_{60} \mathrm{~N}_{60}$ cage has $I_{\mathrm{h}}$ symmetry with 30 squares, 20 hexagons and 12 decagons. Recently, Wu et al. [19, 20] found that the most stable $(\mathrm{BN})_{24}$ isomer has a structure containing two octagons, 16 hexagons and eight squares in $S_{8}$ symmetry, and is computed more stable than the structure by Pokropivny et al. [21] by $60.4 \mathrm{kcal} \mathrm{mol}^{-1}$, but only $2.8 \mathrm{kcal} \mathrm{mol}^{-1}$ more stable than the alternant structure in $S_{4}$ symmetry.

In this paper, we present a B3LYP/6-31G* DFT investigation on the structure and stability of the $(\mathrm{BN})_{36}$ monomer cages. The isomers consist of four-membered $\left(F_{4}\right)$, five-membered $\left(F_{5}\right)$, six-membered $\left(F_{6}\right)$, eightmembered $\left(F_{8}\right)$ and 12-membered ( $F_{12}$ ) rings. The most stable $(\mathrm{BN})_{36}$ is the $T_{\mathrm{d}}$ symmetrical structure with six isolated squares, while the fullerene-like structures ( $12 F_{5}$ and $26 F_{6}$ ) and structures with $F_{8}$ and $F_{12}$ are much higher in energy.

## Computational method

All structures were optimized at the B3LYP/6-31G* density functional level of theory with the Gaussian 98 program [22-25]. Benchmark calculations on $\mathrm{B}_{12} \mathrm{~N}_{12}$ cages showed that the B3LYP results have the same trend as those of HF and MP2 calculations, and B3LYP/6-311 $+\mathrm{G}^{*}$ gives both qualitative and quantitative agreement with B3LYP/6-31G*, and therefore the basis set effect is negligible.

## Results and discussion

## Design principle

To construct ( BN$)_{36}$ cages, it is necessary to gain insight into the relationship between four-membered $\left(F_{4}\right)$, five-
membered $\left(F_{5}\right)$, six-membered $\left(F_{6}\right)$, eight-membered $\left(F_{8}\right)$, and 12-membered ( $F_{12}$ ) -rings in polyhedrons. For cages consisting of $F_{4}$ and $F_{6}$, the number of $F_{4}$ is always equal to $\operatorname{six}\left(F_{4}=6\right)$, whereas the number of $F_{6}$ is $n-4\left(F_{6}=n\right.$ $-4)$. For example, $(\mathrm{BN})_{36}$ have six $F_{4}$ and $32 F_{6}$. This relationship has been used in the literature not only for $(\mathrm{BN})_{\mathrm{n}}$ clusters but also for other systems [26, 27]. On the basis of the constructed structures, the stability of $(\mathrm{BN})_{36}$ isomers depends on the distance of the six $F_{4}$, that is, the larger the distance, the more stable the system, and molecule with maximal distance of the six $F_{4}$ should be the most stable structure, in line with the pentagon rule in fullerene chemistry [28]. On this basis, the number of stable isomers is rather limited, and this will facilitate the computations. However, it is also expected that large cages with well-separated $F_{4}$ can have several isomers very close in energy with reduced torsion strain, and the potential energy surfaces become flat rather than deep. Therefore, the best way for the $(\mathrm{BN})_{\mathrm{n}}$ structures is to start with the configuration having the largest distances of the six $F_{4}$ and then to adjust their relative positions.

## Structure

Isomers $\mathbf{1 - 9}$ in Fig. 1 are isomers with six $F_{4}$ and $32 F_{6}$, and they have one hundred and eight (108) $\mathrm{B}-\mathrm{N}$ bonds, but without direct $\mathrm{B}-\mathrm{B}$ and $\mathrm{N}-\mathrm{N}$ connections. They differ from the location or separation of the $F_{4}$ and $F_{6}$. On the basis of the Aufbau principle discussed above, structure $\mathbf{1}$ with the greatest separation (four $\mathrm{B}-\mathrm{N}$ bonds in zigzag form) and perfect distribution of the six $F_{4}$ in $T_{d}$ symmetry should be the most stable isomer. It is also the structure first reported by Sun et al. [14, 15].

Structure 2 has $C_{3}$ symmetry with the $C_{3}$ axis through the two $F_{6}$ in opposite location. Each $F_{6}$ along the $C_{3}$ axis is connected symmetrically with three $F_{4}$ via $\mathrm{B}-\mathrm{N}$ or $\mathrm{N}-\mathrm{B}$ bond. There are two types of $F_{4}$ separation, one is at the end of the tube by four $\mathrm{B}-\mathrm{N}$ bonds and the second is between the two ends by three $\mathrm{B}-\mathrm{N}$ bonds. Structure 3 has $S_{6}$ symmetry in a discus form, and the location of the $\operatorname{six} F_{4}$ is like in case of $\mathbf{2}$. The separation between $F_{4}$ is three $\mathrm{B}-\mathrm{N}$ bonds. Structure 4 has $C_{2}$ symmetry and the $C_{2}$ axis goes through the centers of two $F_{4}$, which are located at the ends of an ellipsoid form. The other four $F_{4}$ are located in the middle of the ellipsoid form. The separation between $F_{4}$ is three $\mathrm{B}-\mathrm{N}$ bonds.

Structure 5 has $C_{3 \mathrm{~h}}$ symmetry in a triangle form, and the six $F_{4}$ are divided into three groups. Each group is located at the corner of the triangle and the $F_{4}$ separation within the corner is two $\mathrm{B}-\mathrm{N}$ bonds, while four $\mathrm{B}-\mathrm{N}$ bonds between two corners. Structure $\mathbf{6}$ is $C_{1}$ symmetrical and the separation of the six $F_{4}$ has three $\mathrm{B}-\mathrm{N}$ bonds.

Structure 7 has $C_{2}$ symmetry in a rhomboidal form, and the $C_{2}$ axis goes through the centers of two $F_{4}$ located at the trans positions. The other four $F_{4}$ are divided into two groups and they are also located at the trans position, and the two $F_{4}$ within a group are separated by one $\mathrm{B}-\mathrm{N}$ bond. The next one is by four $\mathrm{B}-\mathrm{N}$


Fig. 1 B3LYP/6-31G* optimized $\mathrm{B}_{36} \mathrm{~N}_{36}$ structures with only $F_{4}$ and $F_{6}(\mathbf{1 - 9})$
bonds. Structure $\mathbf{8}$ has $C_{2}$ symmetry in a flat tube form, and the six $F_{4}$ are divided into two groups and located at the ends of the tube. The $F_{4}$ separation at the tube end is one $\mathrm{B}-\mathrm{N}$ bond, while four $\mathrm{B}-\mathrm{N}$ bonds between the ends. Structure 9 has $C_{2 v}$ symmetry in a tube form; the conformation is similar to that of structure 8, one can consider that structure $\mathbf{8}$ can be deduced by rotation the two $F_{4}$ along the $C_{2}$ axis from 9 .

Structures $\mathbf{1 0} \mathbf{- 1 2}$ in Fig. 2 are the corresponding fullerene-like forms with pentagons $\left(F_{5}=12\right)$ and hexagons ( $F_{6}=26$ ) and have three $\mathrm{B}-\mathrm{B}$ and $\mathrm{N}-\mathrm{N}$ bonds. They are also the most stable structures reported by Rogers et al. [17]. The $12 F_{5}$ form six isolated pentagon pairs (IPP), the first three IPP differ from their locations. There are two individual IPP, one with the BB annelation and another one with the $\mathrm{N}-\mathrm{N}$ annelation.

Fig. 2 B3LYP/6-31G*
optimized fullerene-like $\mathrm{B}_{36} \mathrm{~N}_{36}$ structures with $F_{5}$ and $F_{6}$ (10-12)

$12\left(\mathrm{D}_{3}\right) /\left(12 F_{5}+26 F_{6}\right)$

Structure $\mathbf{1 0}$ has $C_{3}$ symmetry in a tube form, and the three IPP with $\mathrm{B}-\mathrm{B}$ annelation are at one end, and the other three IPP with $\mathrm{N}-\mathrm{N}$ annelation are at another end.

The IPP are separated by three $\mathrm{B}-\mathrm{N}$ bonds. Structure 11 also has $C_{3}$ symmetry in discus form, and the separation of the IPP is one B-N bond. Structure $\mathbf{1 2}$ has $D_{3}$ sym-
metry in a discus form, and the shared $\mathrm{B}-\mathrm{B}$ and $\mathrm{N}-\mathrm{N}$ bonds locate at the periphery and the IPP has a separation of one $\mathrm{B}-\mathrm{N}$ bond.

Inspired by the recent work by Pokropivny et al. [21] and Wu et al. $[19,20$ ] that eight-membered rings can stabilize the cage structures, we carried out a set of $\mathrm{B}_{36} \mathrm{~N}_{36}$ isomers containing several $F_{8}$. Structures 13-20 in Fig. 3 are isomers with $F_{4}, F_{6}$ and $F_{8}$. Structure $\mathbf{1 3}$ has seven $F_{4}$, thirty $F_{6}$ and one $F_{8}$, and is $C_{2}$ symmetrical. The $C_{2}$ axis goes through the centers of the $F_{8}$ and one $F_{4}$. Structure 14 is $C_{4 \mathrm{~h}}$ symmetrical and has a tube form with eight $F_{4}, 28 F_{6}$ and two $F_{8}$. The two $F_{8}$ are located at the ends of the tube. This is in agreement with the tube form of $\mathrm{B}_{24} \mathrm{~N}_{24}$ structure [29]. As structure 14, structure $\mathbf{1 5}$ has also eight $F_{4}, 28 F_{6}$ and two $F_{8}$, but in a drum form in $C_{4}$ symmetry.

Structure 16 has $D_{2}$ symmetry with ten $F_{4}, 24 F_{6}$ and four $F_{8}$ in a form of packed luggage with two diagonal belts. The belt around the periphery has eight $F_{4}$ and eight $F_{6}$ in an alternating order, while the orthogonal belt has four $F_{4}$ and four $F_{8}$ in an alternating arrangement. Structure 17 has $D_{2}$ symmetry, and ten $F_{4}, 24 F_{6}$
and four $F_{8}$. The four $F_{8}$ are divided into two groups, one group has two-isolated $F_{8}$ without $F_{4}$ annelations, while another group has two $F_{8}$ and each of them is annelated with four $F_{4}$.

Structure 18 has $S_{4}$ symmetry containing $12 F_{4}, 20 F_{6}$ and six $F_{8}$. There are two $F_{8}$ in annelation with four $F_{4}$, and four $F_{8}$ in annelation with two $F_{4}$. There are two $F_{4}$ bridging two $F_{8}$. Structure 19 has $C_{4}$ symmetry and 12 $F_{4}, 20 F_{6}$ and $\operatorname{six} F_{8}$. There are two $F_{6}$ in annelation with four $F_{4}$ and four $F_{8}$ in annelation with two $F_{4}$, and four $F_{4}$ bridging two $F_{8}$. Structure 20 is $C_{2}$ symmetrical and has $12 F_{4}, 20 F_{6}$ and six $F_{8}$. Each $F_{8}$ is in annelation with two $F_{4}$.

In addition, we have also investigated two structures with 12 -membered rings as shown in Fig. 4. The first one is structure 21, which has $12 F_{4}, 24 F_{6}$ and two $F_{12}$, and is therefore $S_{12}$ symmetrical. Each $F_{12}$ are fused by six $F_{4}$ and six $F_{6}$ alternately. The next example is structure 22, which is $D_{6}$ symmetrical and has $18 F_{4}, 12 F_{6}$, six $F_{8}$ and two $F_{12}$ in a cogwheel form. The $C_{6}$ axis goes through the centers of the two $F_{12}$. The periphery has a belt from six $F_{4}$ and six $F_{8}$, and they are connected alternatively.

Fig. 3 B3LYP/6-31G* optimized $\mathrm{B}_{36} \mathrm{~N}_{36}$ structures with $F_{4}, F_{6}$ and $F_{8}(\mathbf{1 3 - 2 0})$



Fig. $4 \mathrm{~B} 3 \mathrm{LYP} / 6-31 \mathrm{G}^{*}$ optimized $\mathrm{B}_{36} \mathrm{~N}_{36}$ structures with $F_{4}, F_{6}, F_{8}$ and $F_{12}(\mathbf{2 1}-\mathbf{2 2})$

## Stability

Table 1 summarizes the B3LYP/6-31G* total electronic energies, the gap between frontier orbitals (HOMOLUMO) and the relative energies. On the basis of the Aufbau principle, structure 1 with the maximal and perfect separation of the six $F_{4}$ should be the most stable isomer and this is verified by the relative energies in Table 1.

Among the alternant structures $\mathbf{1 - 9}, 1$ is the most stable isomer and the other structures are higher in energy. Interestingly, the difference in relative energy depends on the separation of the $F_{4}$ location. However, it is notable that structures $2-5$ are only higher in energy by less than $10 \mathrm{kcal} \mathrm{mol}^{-1}$. This indicates the reduced torsion strain in these large cage structures, and it is therefore expected that several isomers might co-exist for larger cages, in which the energetic factor of $F_{4}$ in well-located separation does not play the dominant role.

In contrast to the fully alternating isomers $\mathbf{1 - 9}$, the fullerene-like structures ( $\mathbf{1 0}-\mathbf{1 2}$ ) with three $\mathrm{N}-\mathrm{N}$ and three B-B with $12 F_{5}$ forming $26 F_{6}=26$ are higher in energy by about $127-195 \mathrm{kcal} \mathrm{mol}^{-1}$. This energetic order is in sharp contrast to that found by Rogers et al. [17] using the DFTB method, which predicts that the fullerene-like structures ( $\mathbf{1 0} \mathbf{- 1 2}$ ) are more stable than $\mathbf{1 .}$ Although we do not have any explanation for this difference, it seems that the alternant structures are more stable than the fullerene-like isomers.

Structures 13-20 are isomers containing eight-membered rings $\left(F_{8}\right)$. The relative energies in Table 1 indicate that the introduction of $F_{8}$ does not stabilize the cage structure to such an extent to be more stable than the most stable alternant isomer 1, e.g., 13 (with one $F_{8}$ ) as the most stable structures containing $F_{8}$ is $38.9 \mathrm{kcal} \mathrm{mol}^{-1}$ less stable than 1 . Furthermore, the energetic difference among 13-20 does not depend on the number of $F_{8}$. For example, both 14 and 15 have two $F_{8}$, but 14 is more stable than 15 by $414.2 \mathrm{kcal} \mathrm{mol}^{-1}$. Structures $\mathbf{1 6}$ and $\mathbf{1 7}$ with four $F_{8}$, as well as structure 18-20 with six $F_{8}$ are higher in energy than $\mathbf{1 3}$ with one $F_{8}$ and 1 without $F_{8}$.

However, there is obvious evidence for the stability depending on the proximity of $F_{4}$ and $F_{8}$. For example, the two $F_{8}$ in $\mathbf{1 5}$ are not fused with $F_{4}$, but the more stable isomer $\mathbf{1 4}$ with the same ring combination as $\mathbf{1 5}$ has two $F_{8}$ fused with eight $F_{4}$. Even isomer 13 with one $F_{8}$ fused with four $F_{4}$ is more stable than 15 by $305.3 \mathrm{kcal} \mathrm{mol}^{-1}$. The same trend is also found for isomers $\mathbf{1 6}$ and $\mathbf{1 7}$ having the same ring combination; e.g., $\mathbf{1 6}$ with four fused $F_{4}$ and $F_{8}$ is more stable than $\mathbf{1 7}$ without such connection by $192.3 \mathrm{kcal} \mathrm{mol}^{-1}$.

In addition to structures with $F_{8}$, we have also computed two structures (21 and 22) with two $F_{12}$, and they are much higher in energy than 1 and also other alternant isomers (2-9). Therefore, introduction of $F_{12}$, as $F_{8}$, also cannot stabilize the large cages.

At this stage, one might ask the question about the competing effect between the chemical ( $\mathrm{N}-\mathrm{N}, \mathrm{B}-\mathrm{B}$ bonds) and steric (squares) frustration in determining the stable $(\mathrm{BN})_{\mathrm{n}}$ structures. To evaluate the chemical and steric contributions, we have chosen the inorganic boron-nitride model molecules containing $F_{4}$ and $F_{6}$,

Table 1 The B3LYP/6-31G* total electronic ( $E_{\text {tot }}$, au), relative energies $\left(E_{\text {rel }}\right.$, kcal $\mathrm{mol}^{-1}$ ) and the HOMO-LUMO gap $\left(E_{\mathrm{Gap}}, \mathrm{eV}\right)$ as well as the dipole moment ( $\mu$, Debye) of $(\mathrm{BN})_{36}$ isomers

| Isomer | $E_{\text {tot }}$ | $E_{\text {Gap }}$ | $\mu$ | $E_{\text {rel }}$ |
| :--- | :--- | :--- | :--- | :--- |
| $\mathbf{1}\left(T_{\mathrm{d}}\right)$ | -2869.43680 | 5.22 | 0.00 | 0.0 |
| $\mathbf{2}\left(C_{3}\right)$ | -2869.42917 | 6.69 | 0.61 | 4.8 |
| $\mathbf{3}\left(S_{6}\right)$ | -2869.42670 | 6.60 | 0.31 | 6.3 |
| $\mathbf{4}\left(C_{2}\right)$ | -2869.42576 | 6.76 | 0.00 | 6.9 |
| $\mathbf{5}\left(C_{3 \mathrm{~h}}\right)$ | -2869.42136 | 6.33 | 0.00 | 9.7 |
| $\mathbf{6}\left(C_{1}\right)$ | -2869.41936 | 6.45 | 1.58 | 10.9 |
| $\mathbf{7}\left(C_{2}\right)$ | -2869.34421 | 6.26 | 0.36 | 58.1 |
| $\mathbf{8}\left(C_{2}\right)$ | -2869.31454 | 6.54 | 1.02 | 76.7 |
| $\mathbf{9}\left(C_{2 v}\right)$ | -2869.21833 | 5.59 | 1.09 | 137.1 |
| $\mathbf{1 0}\left(C_{3}\right)$ | -2869.23431 | 4.78 | 1.65 | 127.1 |
| $\mathbf{1 1}\left(C_{3}\right)$ | -2869.19567 | 4.97 | 1.47 | 151.3 |
| $\mathbf{1 2}\left(D_{3}\right)$ | -2869.12563 | 0.00 | 4.90 | 195.3 |
| $\mathbf{1 3}\left(C_{2}\right)$ | -2869.37475 | 0.12 | 6.28 | 38.9 |
| $\mathbf{1 4}\left(C_{4 \mathrm{~h}}\right)$ | -2869.38905 | 0.00 | 6.30 | 30.0 |
| $\mathbf{1 5}\left(C_{4}\right)$ | -2868.72896 | 1.89 | 6.42 | 444.2 |
| $\mathbf{1 6}\left(D_{2}\right)$ | -2869.06847 | 0.00 | 6.05 | 231.1 |
| $\mathbf{1 7}\left(D_{2}\right)$ | -2868.76210 | 0.00 | 6.00 | 423.4 |
| $\mathbf{1 8}\left(S_{4}\right)$ | -2869.16018 | 0.00 | 6.19 | 173.6 |
| $\mathbf{1 9}\left(C_{4}\right)$ | -2869.18865 | 0.13 | 6.05 | 155.7 |
| $\mathbf{2 0}\left(C_{2}\right)$ | -2869.10484 | 0.12 | 6.09 | 208.3 |
| $\mathbf{2 1}\left(S_{12}\right)$ | -2869.13573 | 0.00 | 6.14 | 188.9 |
| $\mathbf{2 2}\left(D_{6}\right)$ | -2868.91236 | 0.00 | 6.01 | 329.1 |

and these model systems can isomerize to the corresponding systems containing $F_{5}$ and $F_{6}$ with one $\mathrm{B}-\mathrm{B}$ bond and one $\mathrm{N}-\mathrm{N}$ bond. The isomerization energy of these models can reveal the difference between the steric frustration of one $F_{4}$ and one $F_{6}$ and the chemical frustration of two $F_{5}$. As shown in Fig. 5, the isomerizaton energy for the pentalene-type molecule (b) is $76.9 \mathrm{kcal} \mathrm{mol}^{-1}$, and that of the s-indacene-type molecule (d) is $73.6 \mathrm{kcal} \mathrm{mol}^{-1}$ (both planar b and d are used for the energetic evaluation, because the non-planar $b$ and d with pyramidal nitrogen centers at the $\mathrm{N}-\mathrm{B}$ bond are only less than $1.5 \mathrm{kcal} \mathrm{mol}^{-1}$ more stable than the planar forms at the same level of theory). These energetic data indicate that the chemical frustration is less favored than the steric frustration and provide additional evidence for the enhanced stability of the alternant structure. It is to be expected that large systems, in which all the $12 F_{5}$ are "isolated" and do not perturb to each other, are still higher in energy than the alternant isomers with six isolated $F_{6}$. On the basis of this analysis, it can be concluded that the discrepancy between DFT and DFTB might be a problem of insufficient DFTB parameters, which should be improved further. On the other hand, there is no direct relationship between dipole moment and the stability, and most of the isomers do not have or have only very small dipole moments because of their high symmetries. Thus, dipole moments do not determine the relative stability.

Apart from this energetic difference, the stability of the alternant can be governed by the stabilizing charge effects of the electropositive charged boron atoms and the electronegative charged nitrogen atoms despite the large strain in $F_{4}$. In contrast, $\mathrm{B}-\mathrm{B}$ and $\mathrm{N}-\mathrm{N}$ bonds have destabilizing rather than stabilizing effects. This is shown in Fig. 6 by the computed natural charges for A and B from a Natural Bond Orbital Analysis [30, 31]. Similar results are also found for C and D.


Fig. 5 Isomerization energy from $F_{4}$ and $F_{6}$ structure into two $F_{5}$ structure

a

b

Fig. 6 Computed natural charges at boron and nitrogen centers

## Conclusion

The relationship between structure and stability of $(\mathrm{BN})_{36}$ cages structures has been computed at the B3LYP/6-31G* level of theory. The most stable isomer (1) is that with 32 hexagons $\left(F_{6}\right)$ and six squares $\left(F_{4}\right)$, and the six $F_{4}$ have their maximal separations. Other alterant structures are higher in energy. In contrast to the findings by Rogers et al., structure (1) is more stable than the fullerene-like isomers with three $\mathrm{B}-\mathrm{B}$ and three $\mathrm{N}-\mathrm{N}$ bonds. The origin of the enhanced stability of the alternant structure is the strong electrostatic interaction between boron and nitrogen in the alternating way, and this stabilizing contribution suppresses the strain (or steric) effects by the squares. Structures with large-sized rings ( $F_{8}$ and $F_{12}$ ) are also higher in energy than the alternant structure.

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